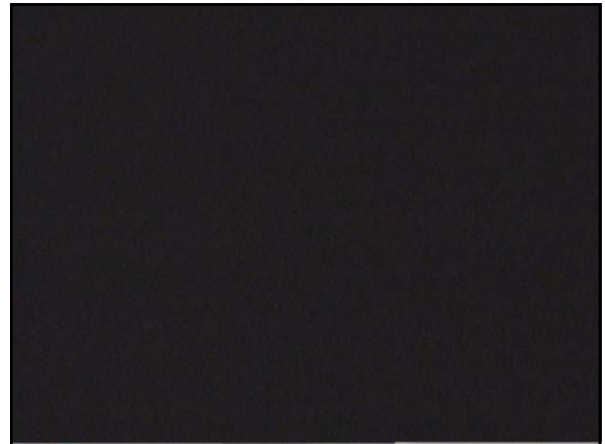


Movie Segment

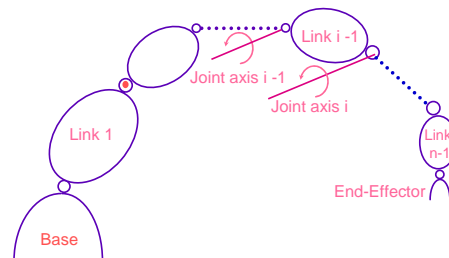
The Hummingbird, IBM Watson Research Center, ICRA 1992 video proceedings



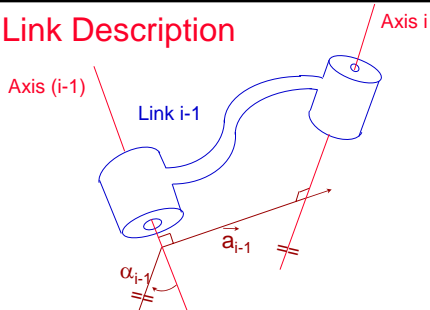
Manipulator Kinematics

- Link Description
- Denavit-Hartenberg Notation
- Frame Attachment
- Forward Kinematics

Manipulator



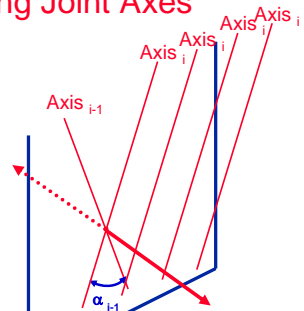
Link Description



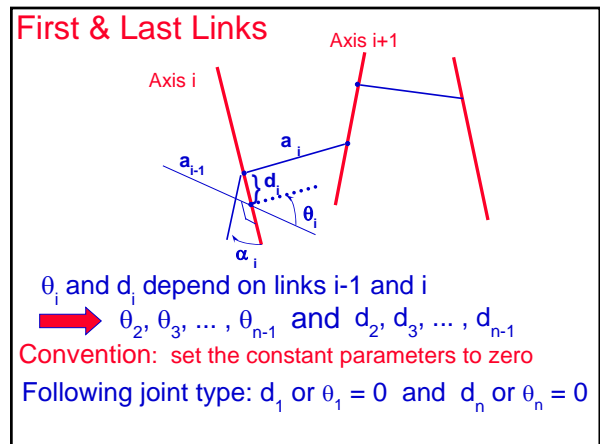
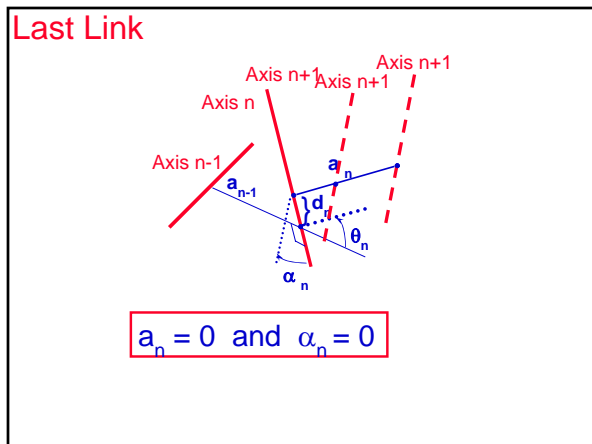
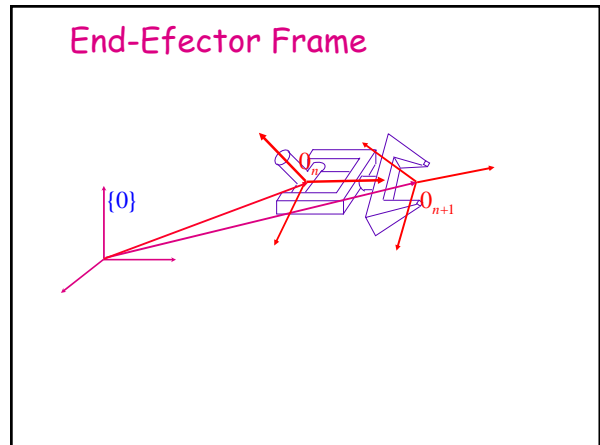
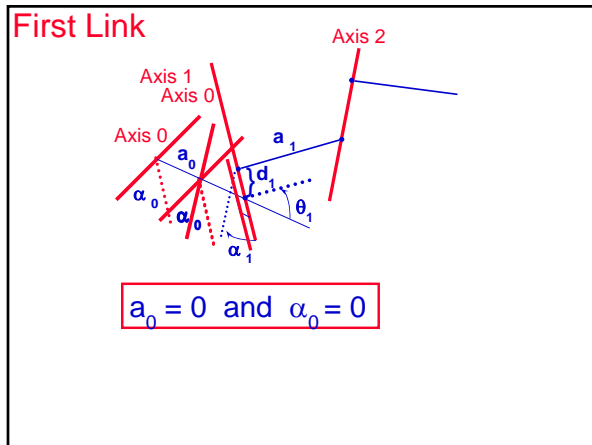
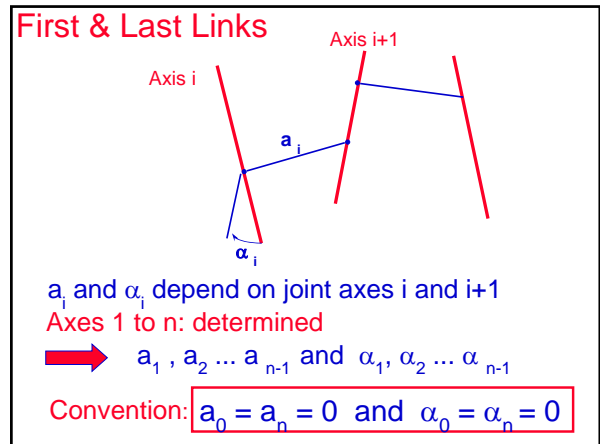
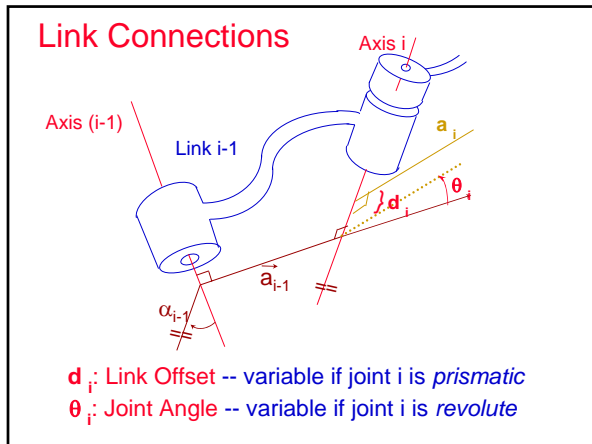
a_{i-1} : Link Length - mutual perpendicular
unique except for parallel axis

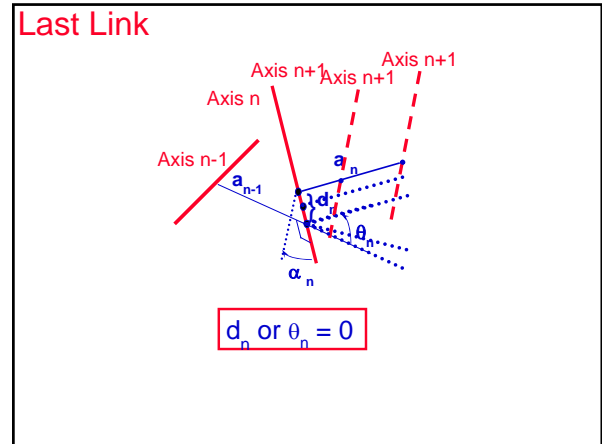
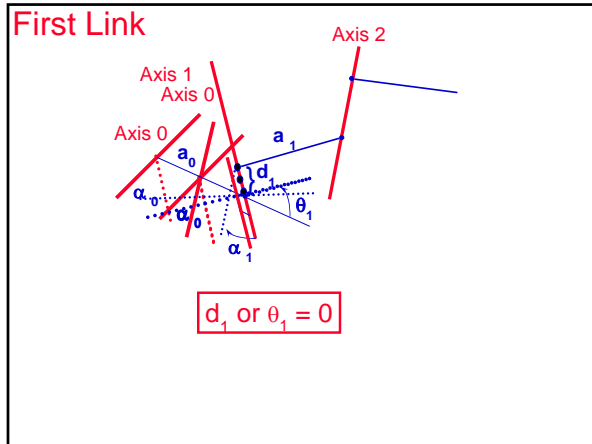
α_{i-1} : Link Twist - measured in the right-hand sense about \vec{a}_{i-1}

Intersecting Joint Axes



The sense of α_{i-1} is free





Denavit-Hartenberg Parameters

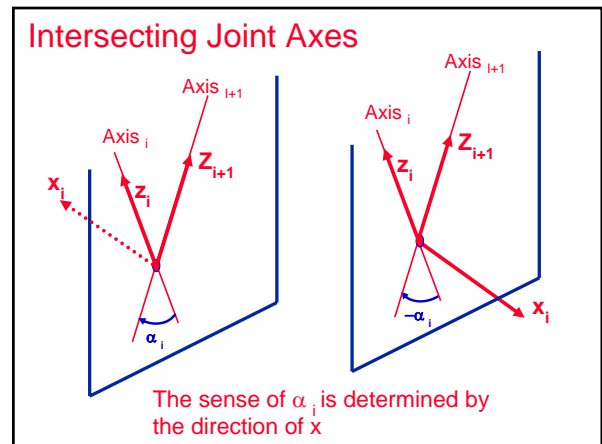
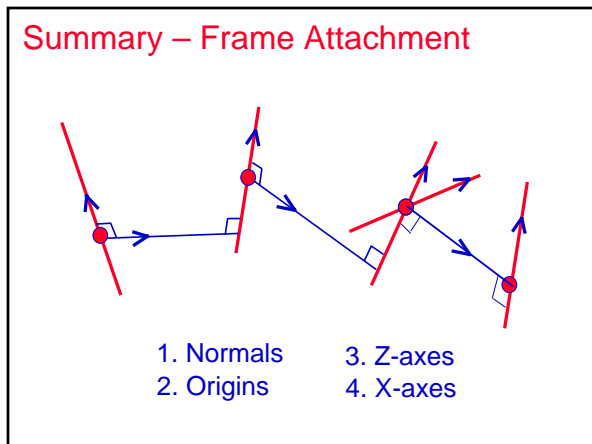
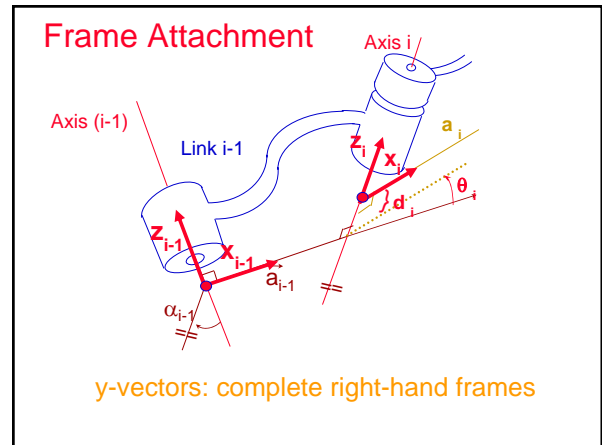
4 D-H parameters ($\alpha_i, a_i, d_i, \theta_i$)

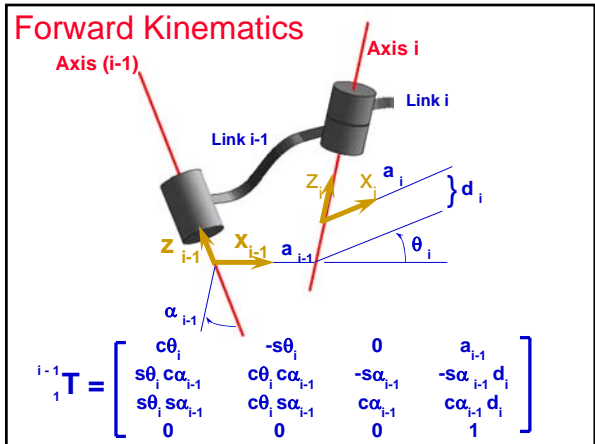
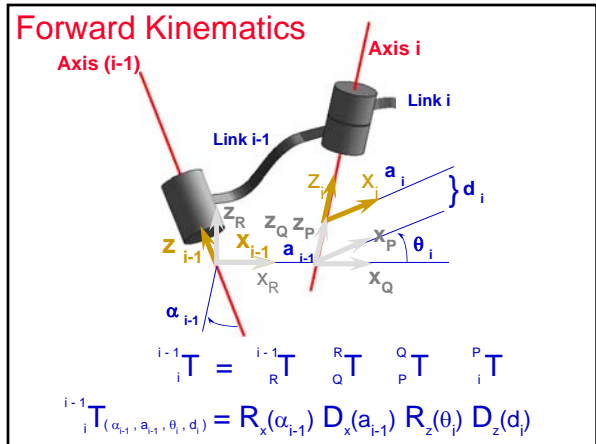
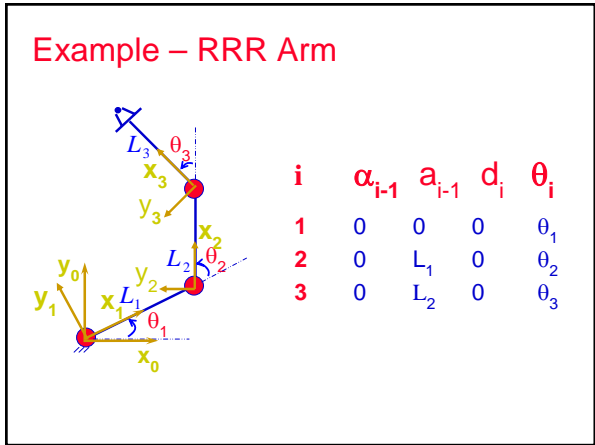
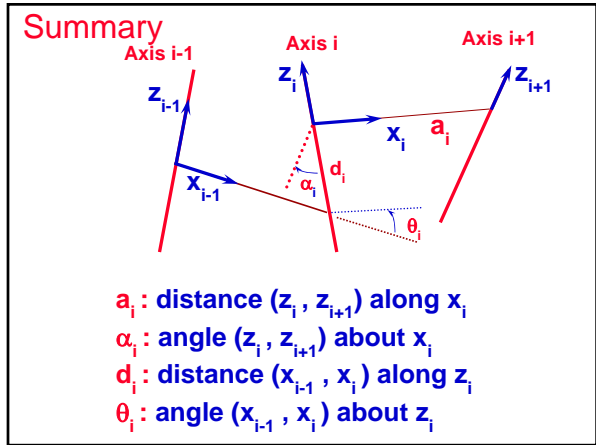
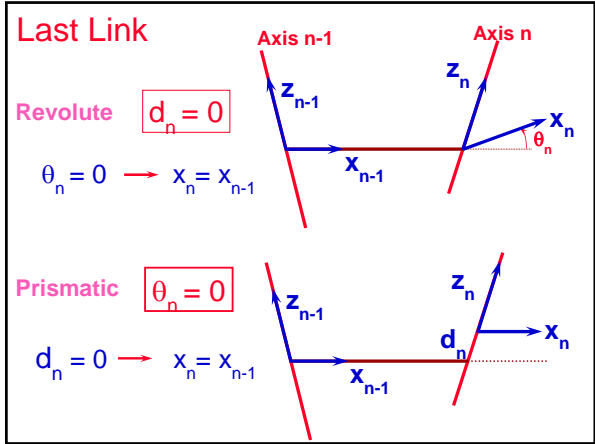
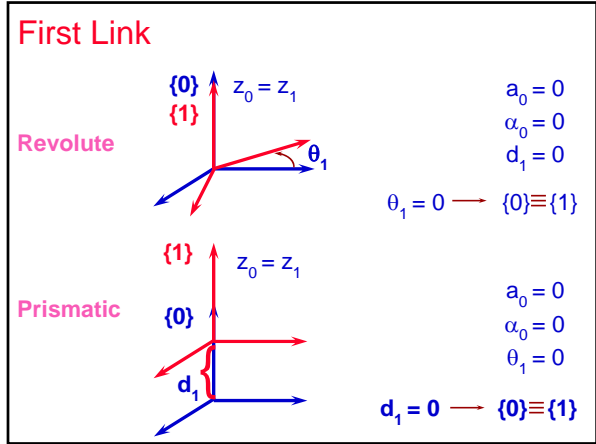
3 fixed link parameters

1 joint variable $\left\{ \begin{array}{l} \theta_i \text{ revolute joint} \\ d_i \text{ prismatic joint} \end{array} \right.$

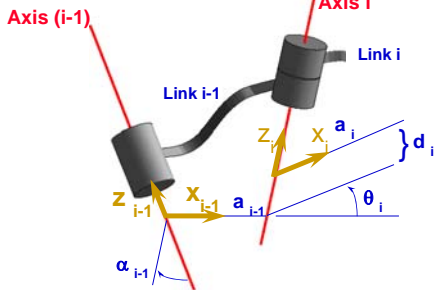
α_i and a_i : describe the Link i

d_i and θ_i : describe the Link's connection





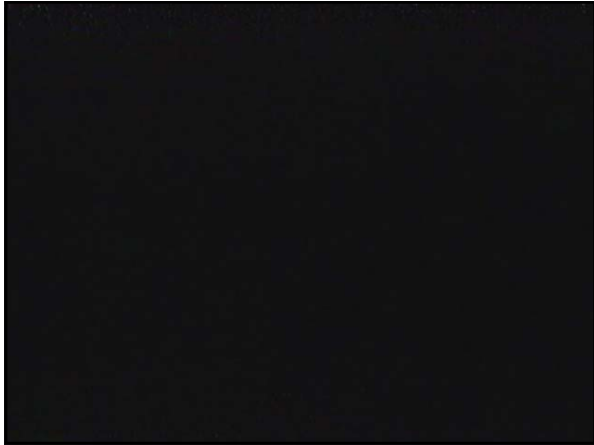
Forward Kinematics



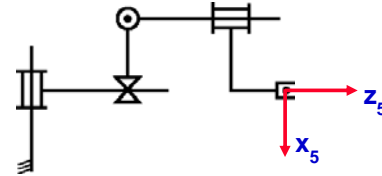
Forward Kinematics: ${}^0_N T = {}^0_1 T \cdot {}^1_2 T \cdot \dots \cdot {}^{N-1}_N T$

Movie Segment

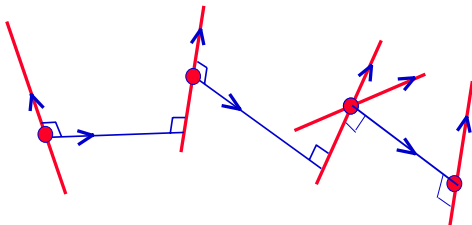
Brachiation Robot, Nagoya University, ICRA 1993 video proceedings



Example - RPRR

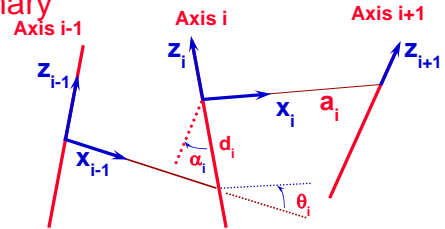


Summary – Frame Attachment



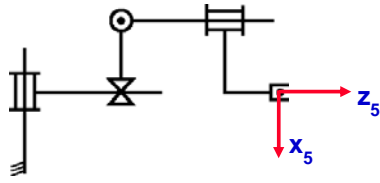
1. Normals
2. Origins
3. Z-axes
4. X-axes

Summary

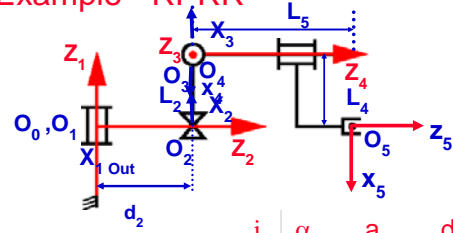


- a_i : distance (z_i, z_{i+1}) along x_i
- α_i : angle (z_i, z_{i+1}) about x_i
- d_i : distance (x_{i-1}, x_i) along z_i
- θ_i : angle (x_{i-1}, x_i) about z_i

Example - RPRR



Example - RPRR



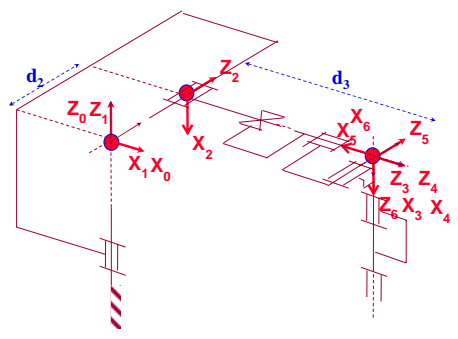
| i | α_{i-1} | a_{i-1} | d_i | θ_i |
|-----|----------------|-----------|-------|------------|
| 1 | 0 | 0 | 0 | θ_1 |
| 2 | -90 | 0 | d_2 | -90 |
| 3 | -90 | L_2 | 0 | θ_3 |
| 4 | 90 | 0 | L_5 | θ_4 |
| 5 | 0 | L_4 | 0 | 0 |

a_i : distance (z_i, z_{i+1}) along x_i
 α_i : angle (z_i, z_{i+1}) about x_i
 d_i : distance (x_{i-1}, x_i) along z_i
 θ_i : angle (x_{i-1}, x_i) about z_i

Stanford Scheinman Arm



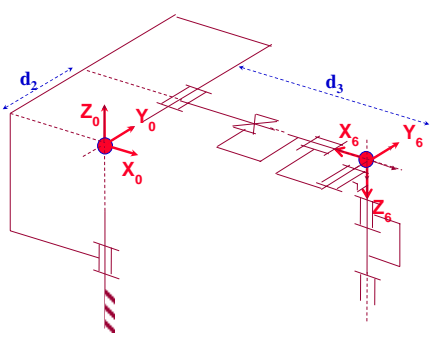
Stanford Scheinman Arm

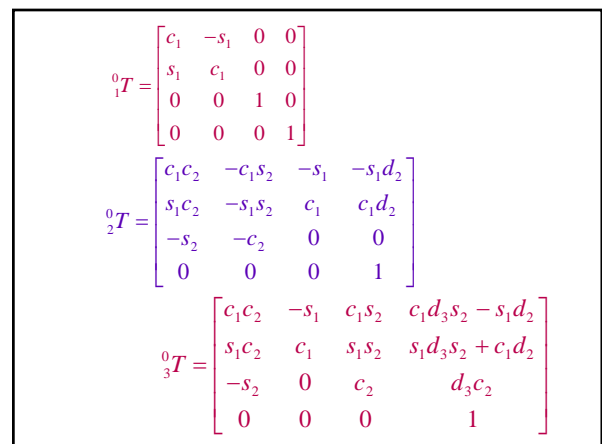
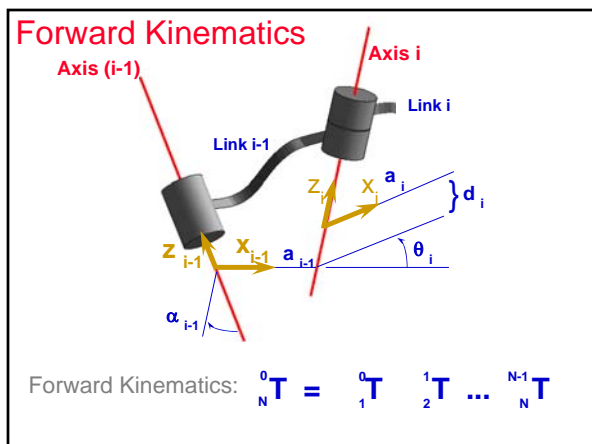
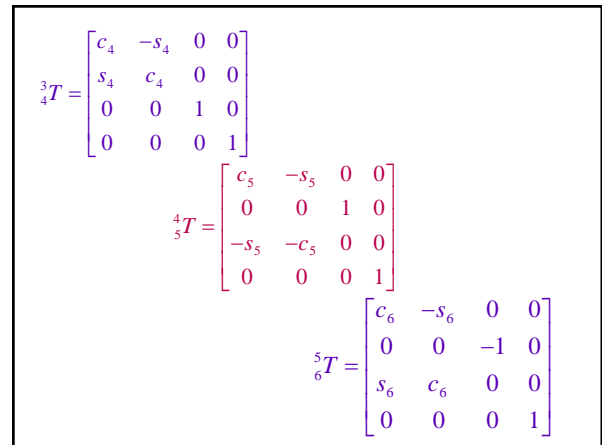
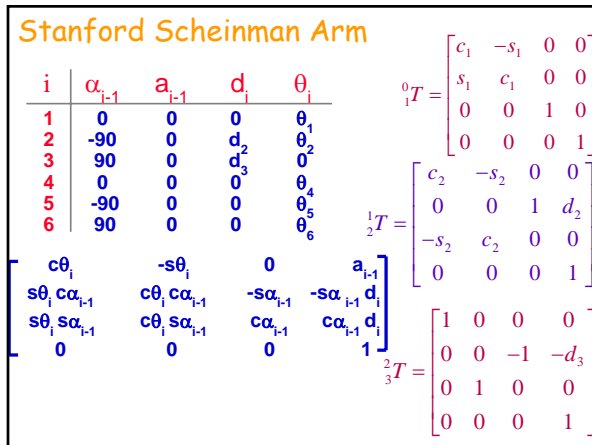
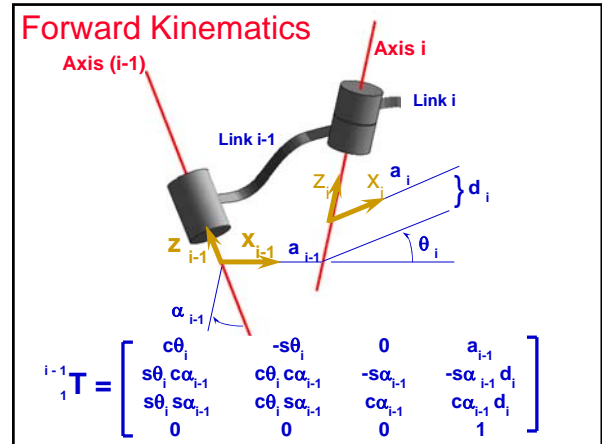
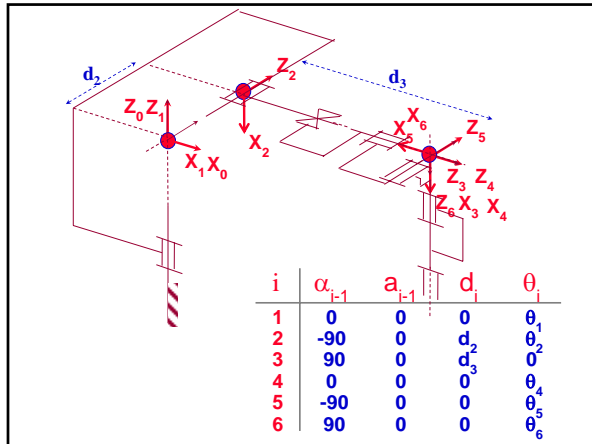


| i | α_{i-1} | a_{i-1} | d_i | θ_i |
|-----|----------------|-----------|-------|------------|
| 1 | 0 | 0 | 0 | θ_1 |
| 2 | -90 | 0 | d_2 | θ_2 |
| 3 | 90 | 0 | d_3 | θ_4 |
| 4 | 0 | 0 | 0 | θ_5 |
| 5 | -90 | 0 | 0 | θ_6 |
| 6 | 90 | 0 | 0 | |

a_i : distance (z_i, z_{i+1}) along x_i
 α_i : angle (z_i, z_{i+1}) about x_i
 d_i : distance (x_{i-1}, x_i) along z_i
 θ_i : angle (x_{i-1}, x_i) about z_i

Stanford Scheinman Arm





$${}^0_4T = \begin{bmatrix} c_1c_2c_4 - s_1s_4 & -c_1c_2s_4 - s_1c_4 & c_1s_2 & c_1d_3s_2 - s_1d_2 \\ s_1c_2c_4 + c_1s_4 & -s_1c_2s_4 + c_1c_4 & s_1s_2 & s_1d_3s_2 + c_1d_2 \\ -s_2c_4 & s_2s_4 & c_2 & d_3c_2 \\ 0 & 0 & 0 & 1 \end{bmatrix}$$

$${}^0_5T = \begin{bmatrix} X & X & -c_1c_2s_4 - s_1c_4 & c_1d_3s_2 - s_1d_2 \\ X & X & -s_1c_2s_4 + c_1c_4 & s_1d_3s_2 + c_1d_2 \\ X & X & s_2s_4 & d_3c_2 \\ 0 & 0 & 0 & 1 \end{bmatrix}$$

$${}^0_6T = \begin{bmatrix} X & X & c_1c_2c_4s_5 - s_1s_4s_5 + c_1s_2s_5 & c_1d_3s_2 - s_1d_2 \\ X & X & s_1c_2c_4s_5 + c_1s_4s_5 + s_1s_2c_5 & s_1d_3s_2 + c_1d_2 \\ X & X & -s_2c_4s_5 + c_2c_5 & d_3c_2 \\ 0 & 0 & 0 & 1 \end{bmatrix}$$

